FST 2-5 Notes

Topic: Exponential Models

GOAL

Construct mathematical models of situations that are exponential in nature. Given two points of such a model, find an equation of the form $y = ab^x$ by solving a system of two equations with two unknowns.

SPUR Objectives

F Find and interpret exponential regression and models.

Vocabulary

exponential regression half-life

1. The population of a certain cell type was observed to be 100 on the second day, and 2700 on the fifth day. Assuming the growth is exponential, find the number of cells present initially, and the number of cells expected on the seventh day.

number of cells expected on the seventh day. $y = a \cdot b$ $\begin{array}{c|c}
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X & y \\
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X & y \\
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Subtract < 2 & 100 & Divide \\
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5 & 2700 & Divide \\
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 $y = a \cdot b^{2}$ $y = a \cdot b^{2}$ y = 2. The National Science Foundation (NSF) publishes InfoBriefs, a newsletter containing brief reports highlighting results from recent surveys and analyses. The following data are contained in a January 2009 article about Federal R&D funding.

a. Use a statistics utility to graph the data and fit an exponential model of the form $f(x) = ab^x$ to the data. Use x as "years in the exponential model to the nearest

2 1998 1999 after 1990." Report the values of a and b **2000** 2001 thousandth. 12 2002 13 2003 data already in L1, L2 14 2004 view scatter plot 2nd - STAT PLOT **5** 2005 6 2006 7 2007 observe scatter plot - does data appear linear? exponential?

find exponential model. STAT - CALC - 0:ExpReg (enter)

Y=151.7631579x+1423.552632 7 Calc #0 Y = 1625.159687 (1.05647444)b. Use your graph to describe how well the

exponential curve you have modeled fits the points on the scatterplot. Go to Y = enter equations

(\$ millions)

1690

1785

1868

1882

2040

2149

2188

2249

2289

2506

2726

3044

3260 3609

3771

3743

3791 4051

1990

1991

1992

1993

1994

1995

1996

7 1997

Linear = $\leq x^2 = 608,006.658$ Exponential $\leq x^2 = 321,953.726$ best fit because smaller squared residuals

c. Calculate the residuals for 1998 and 2004.

find ordered pairs (predicted values) for model: 2nd TABLE

adjust table: 2nd TBLSET (TbleStart = ____)

$$y = a \cdot b^{\times}$$
 $y = \text{end value}$
 $a = \text{start value}$
 $b = \text{growth/decay}$ factor
 $b = \text{grams is being observed, how much will remain in 50 years? When will only 5 grams remain?}$
 $y = a \cdot b^{\times}$
 $y =$

95.89 yrs = X